# Lecture

# Sensor Technology

EE 565: Position, Navigation and Timing

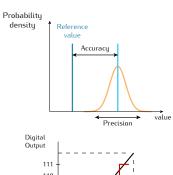
Lecture Notes Update on Spring 2023

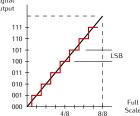
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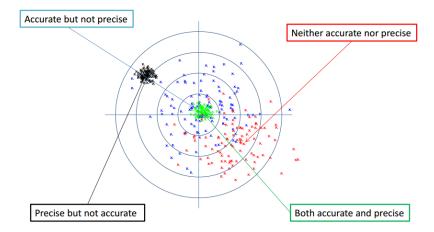
## **Terminology**

- Accuracy: Proximity of the measurement to the true value
- Precision: The consistency with which a measurement can be obtained
- Resolution: The magnitude of the smallest detectable change
- **Sensitivity:** The ratio between the change in the output signal to a small change in input physical signal. Slope of the input-output fit line.
- Linearity: the deviation of the output from a "best" straight line fit for a given range of the sensor





### Accuracy vs Precision



### Inertial Sensors — Bias Errors

• Bias — often the most critical error

- Fixed Bias  $b_{FB}$ 
  - \* Deterministic in nature and can be addressed by calibration
  - \* Often modeled as a function of temperature
- Bias Stability  $b_{BS}$ 
  - \* Varies from run-to-run as a random constant
- Bias Instability  $b_{BI}$ 
  - \* In-run bias drift typically modeled as random walk

#### Bias Errors

$$\Delta f = b_{a,FB} + b_{a,BI} + b_{a,BS} = b_a$$

$$\Delta\omega = b_{g,FB} + b_{g,BI} + b_{g,BS} = b_g$$

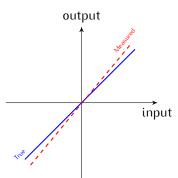
# Inertial Sensors — Scale Factor Errors

- Fixed scale factor error
  - Deterministic in nature and can be addressed by calibration
  - Often modeled as a function of temperature
- ullet Scale Factor Stability  $s_a$  (accel) or  $s_g$  (gyro)
  - Varies from run-to-run as a random constant
  - Typically given in parts-per-million (ppm)

#### Scale Factor Errors

$$\Delta f = s_a f, \qquad \Delta \omega = s_g \omega$$

The scale factor represents a linear approximation to the steady-state sensor response over a given input range — True sensor response may have some non-linear characteristics



#### Inertial Sensors — Misalignment

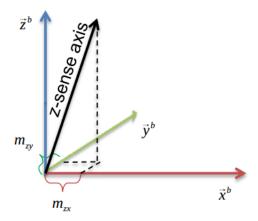
- Refers to the angular difference between the ideal sense axis alignment and true sense axis vector
  - a deterministic quantity typically given in milliradians

$$\Delta f_z = m_{a,zx} f_x + m_{a,zy} f_y$$

$$\Delta\omega_z = m_{q,zx}\omega_x + m_{q,zy}\omega_y$$

• Combining misalignment & scale factor

$$\Delta \vec{f} = \begin{bmatrix} s_{a,x} & m_{a,xy} & m_{a,xz} \\ m_{a,yx} & s_{a,y} & m_{a,yz} \\ m_{a,zx} & m_{a,zy} & s_{a,z} \end{bmatrix} \begin{bmatrix} f_x \\ f_y \\ f_z \end{bmatrix} = M_a \vec{f}_{ib}^b$$



### Inertial Sensors — Cross-Axis Response

- Refers to the sensor output which occurs when the device is presented with a stimulus which is vectorially orthogonal to the sense axis
- Misalignment and cross-axis response are often difficult to distinguish Particularly during testing and calibration activities

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#### Inertial Sensors — Other Noise Sources

Typically characterized as additive in nature

- May have a compound form
  - white noise
    - \* Gyros: white noise in rate  $\Rightarrow$  Angle Random Walk (ARW)
    - \* Accels: white noise in accel ⇒ Velocity Random Walk (VRW)

- Quantization noise
  - \* May be due to LSB resolution in ADC's
- Flicker noise
- Colored noise

## Inertial Sensors — Gyro Specific Errors

- G-sensitivity
  - The gyro may be sensitive to acceleration
  - Primarily due to device mass assymetry
  - Mostly in Coriolis-based devices (MEMS)

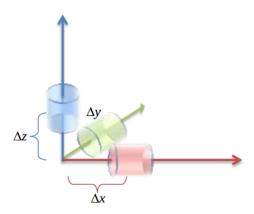
$$\Delta \vec{\omega}_{ib}^{\ b} = G_a \vec{f}_{ib}^{\ b} a$$

- G<sup>2</sup>-Sensitivity
  - Anisoelastic effects
  - Due to products of orthogonal forces

#### Inertial Sensors — Accel Specific Errors

- Axis Offset
  - The accel may be mounted at a lever-arm distance from the "center" of the Inertial Measurement Unit (IMU)
    - \* Leads to an " $\omega^2 r$ " type effect

$$\Delta f_x = \omega_y^2 \Delta x + \omega_z^2 \Delta x = (\omega_y^2 + \omega_z^2) \Delta x$$



#### Inertial Sensors — Sensor Models

• Accelerometer model

$$\tilde{\vec{f}}_{ib}^{b} = \vec{f}_{ib}^{b} + \Delta \vec{f}_{ib}^{b} = \vec{b}_a + (\mathcal{I} + M_a) \vec{f}_{ib}^{b} + \vec{w}_a \tag{1}$$

• Gyro Model

$$\tilde{\vec{\omega}}_{ib}^{\ b} = \vec{\omega}_{ib}^{\ b} + \Delta \vec{\omega}_{ib}^{\ b} = \vec{b}_g + (\mathcal{I} + M_g) \vec{\omega}_{ib}^{\ b} + G_g \vec{f}_{ib}^{\ b} + \vec{w}_g$$
 (2)

• Typically, each measures along a signle sense axis requiring three of each to measure the 3-tupple vector

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