

Assimilation of Earth Rotation Parameters into the Community Atmosphere Model

Lisa Neef^{1,3} & Katja Matthes^{1,2,3}

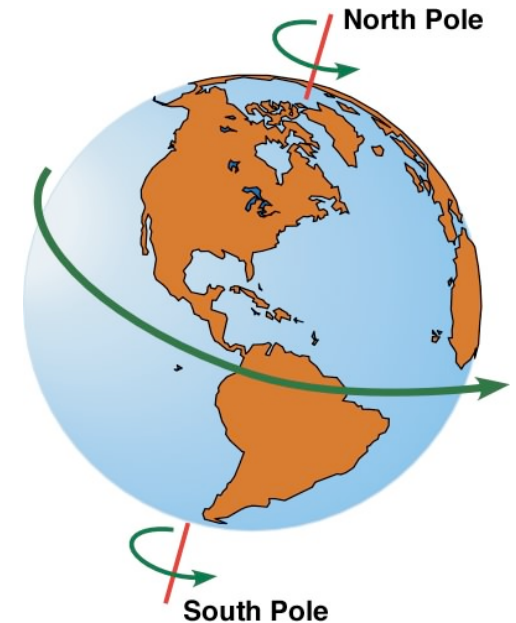
¹Helmholtz Centre for Geosciences Potsdam (GFZ)

²Free University of Berlin

³ now at Helmholtz Centre for Ocean Research Kiel (GEOMAR)

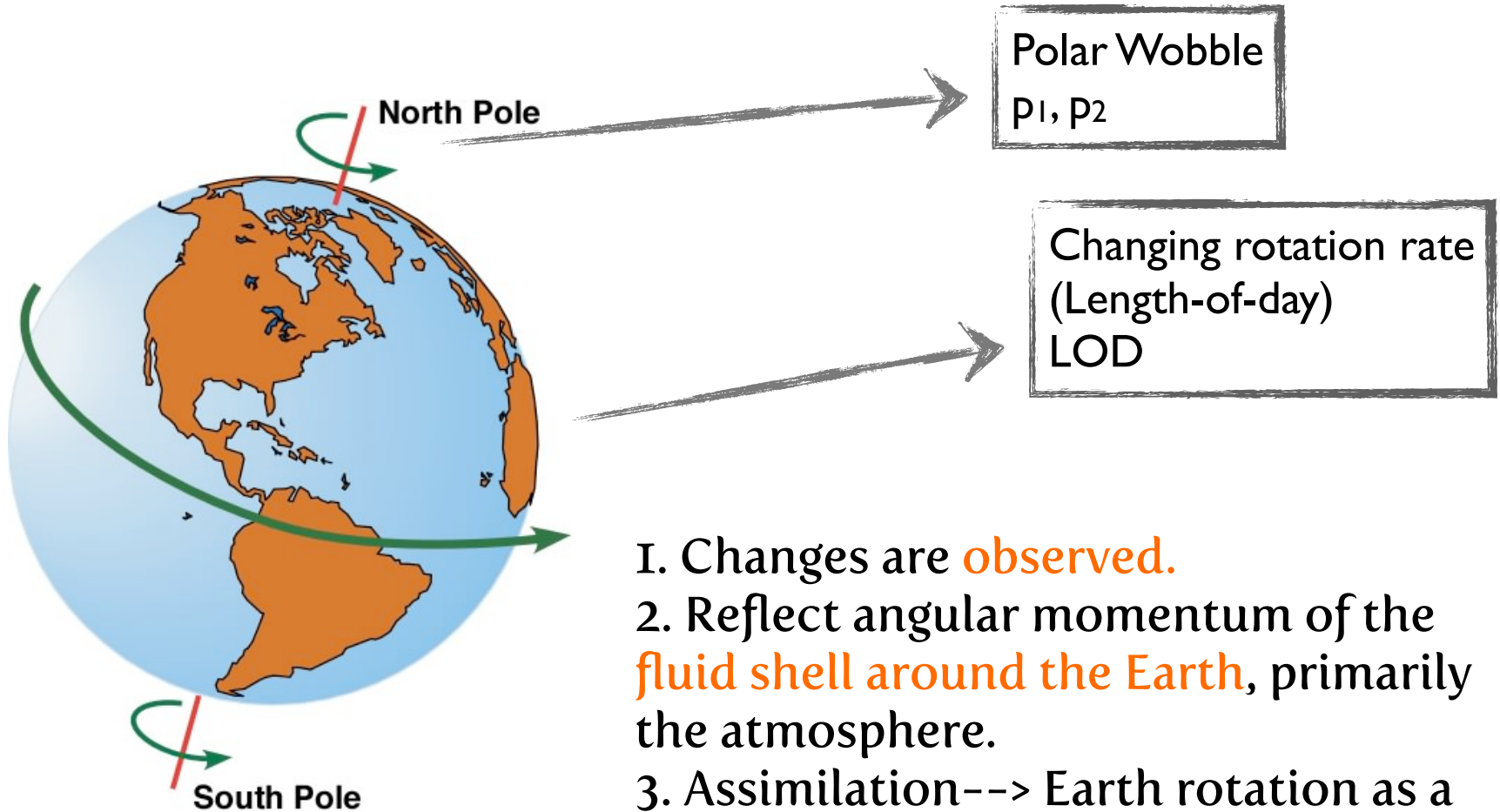
2012 SPARC Data Assimilation Workshop

Socorro, New Mexico



Motivation

Earth rotation varies in time.



Polar Wobble

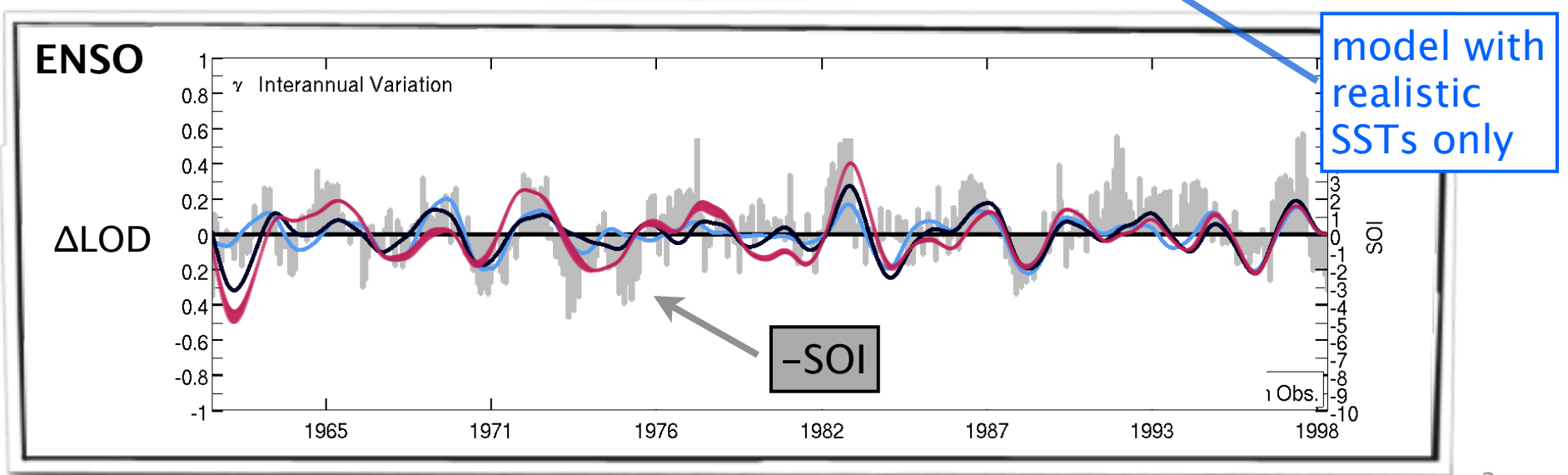
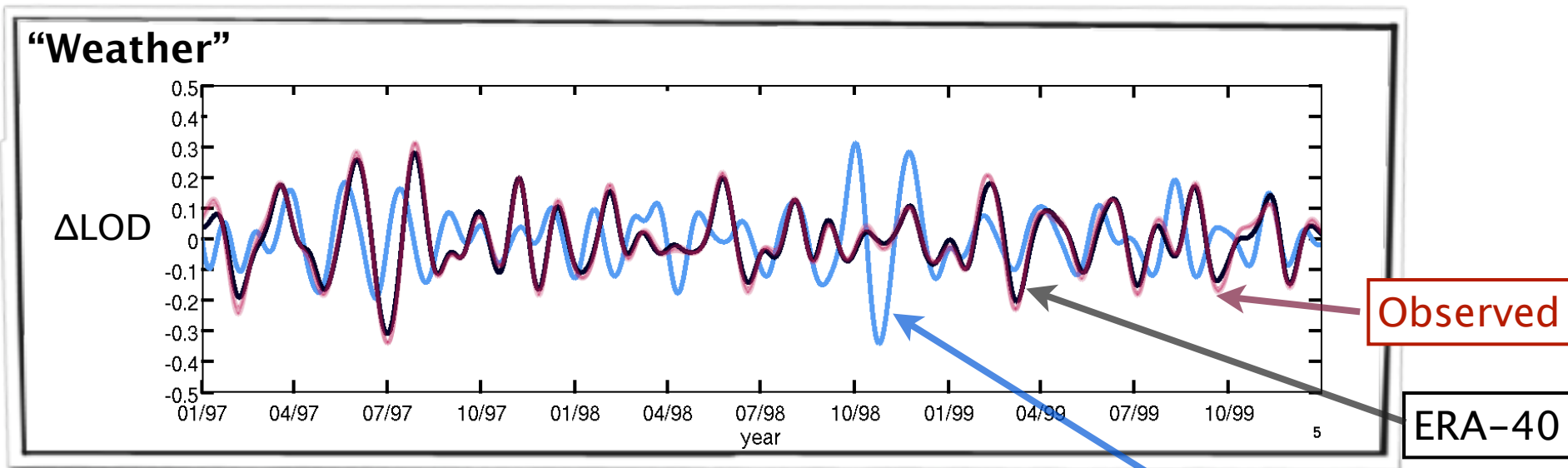
p_1, p_2

Changing rotation rate
(Length-of-day)

LOD

1. Changes are **observed**.
2. Reflect angular momentum of the **fluid shell around the Earth**, primarily the atmosphere.
3. Assimilation--> Earth rotation as a **constraint upon atmosphere** models.

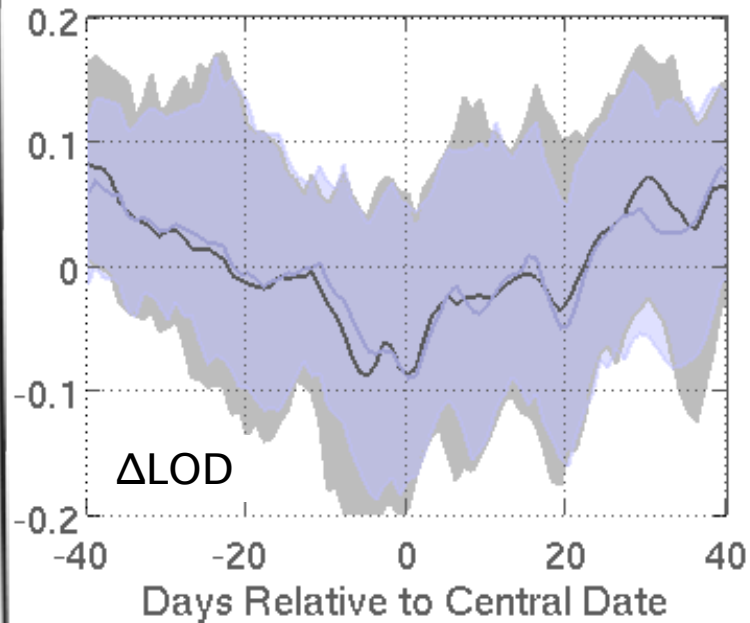
Atmospheric Effects on Earth Rotation (Examples)



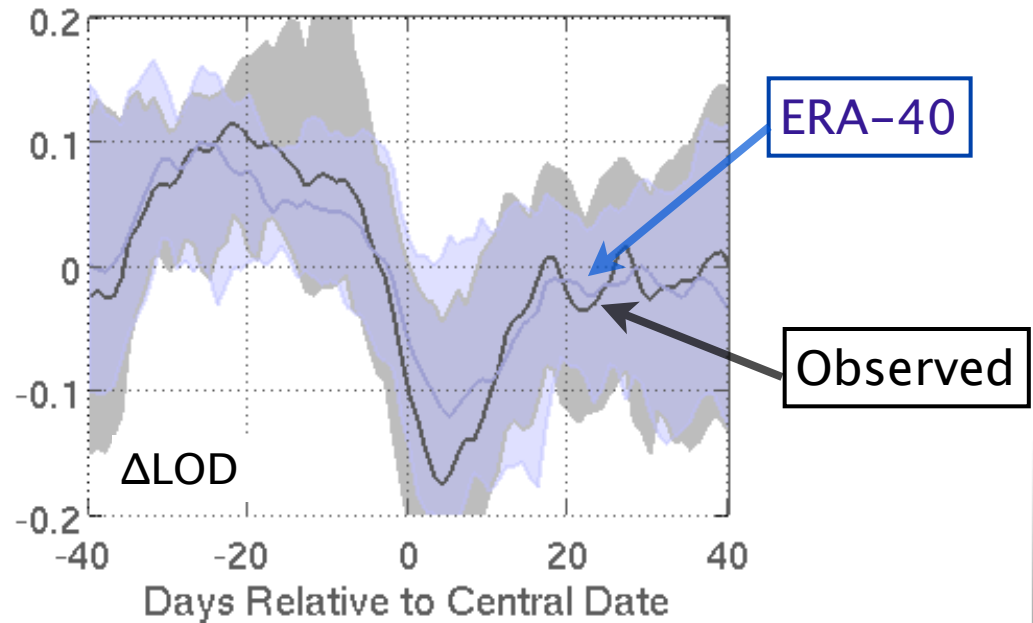
Atmospheric Effects on Earth Rotation (Examples)

Sudden Stratospheric Warmings

Displacement



Split



Also:

NAM/SAM (Petrick et al., 2012; Marcus et al., 2012)

Blocking (Neef and Walther, in progress.)

MJO (Dickey et al., 1991)

Excitation of Earth Rotation by Angular Momentum Exchange

Polar Motion components

$$p_1 + \frac{\dot{p}_2}{\sigma_0} = \chi_1$$
$$-p_2 + \frac{\dot{p}_1}{\sigma_0} = \chi_2$$

Equatorial excitation functions

Length-of-day changes

$$\frac{\Delta\text{LOD}}{\text{LOD}_0} = \Delta\chi_3$$

Axial excitation

Atmospheric Excitation of Earth Rotation

Earth
Rotation
Variations

~

Variations in Atmospheric Angular
Momentum

$$\begin{aligned}
 p_1 + \frac{\dot{p}_2}{\sigma_0} &= \chi_1 = -\frac{R^3}{g(C-A)} \left[\frac{1.16}{\Omega} \int \int \int (u \sin \phi \cos \phi \cos \lambda - v \cos \phi \sin \lambda) d\lambda d\phi dp \right] && 1.10R \int \int p_s \sin \phi \cos^2 \phi \cos \lambda d\lambda d\phi \\
 -p_2 + \frac{\dot{p}_1}{\sigma_0} &= \chi_2 = -\frac{R^3}{g(C-A)} \left[\frac{1.61}{\Omega} \int \int \int (u \sin \phi \cos \phi \sin \lambda + v \cos \phi \cos \lambda) d\lambda d\phi dp \right] && 1.10R \int \int p_s \sin \phi \cos^2 \phi \sin \lambda d\lambda d\phi \\
 \frac{\Delta \text{LOD}}{\text{LOD}_0} &= \chi_3 = \frac{R^3}{C_m g} \left[\frac{0.997}{\Omega} \int \int \int u \cos^2 \phi d\lambda d\phi dp \right] && R \int \int p_s \cos^3 \phi d\lambda d\phi
 \end{aligned}$$

Earth
Rotation
Variations

=

Motion
(relative AM)

+

Mass
(moment of
inertia)

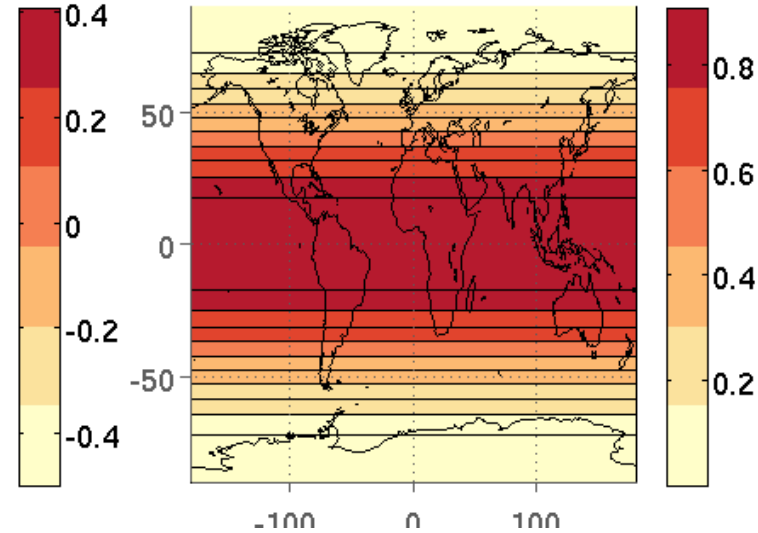
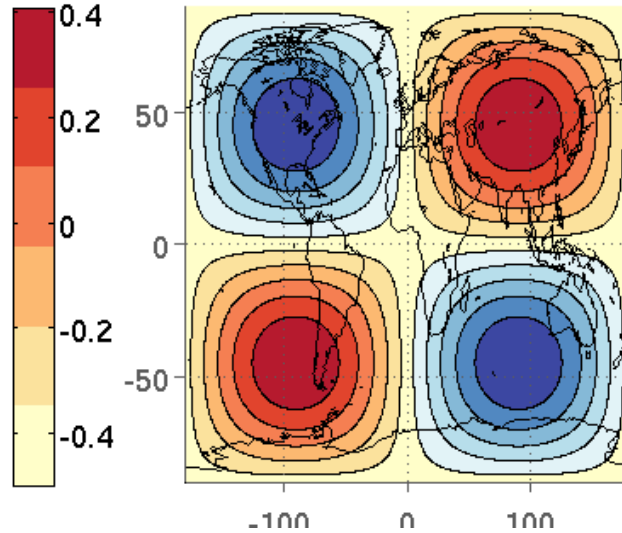
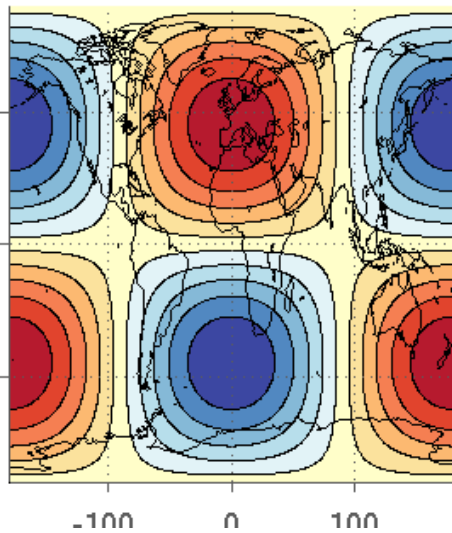
Geographic Weighting Functions

$$\begin{aligned}
 p_1 + \frac{\dot{p}_2}{\sigma_0} &= \chi_1 = -\frac{R^3}{g(C-A)} \left[\frac{1.16}{\Omega} \int \int \int (u \sin \phi \cos \phi \cos \lambda - v \cos \phi \sin \lambda) d\lambda d\phi dp + 1.10R \int \int p_s \sin \phi \cos^2 \phi \cos \lambda d\lambda d\phi \right] \\
 -p_2 + \frac{\dot{p}_1}{\sigma_0} &= \chi_2 = -\frac{R^3}{g(C-A)} \left[\frac{1.61}{\Omega} \int \int \int (u \sin \phi \cos \phi \sin \lambda + v \cos \phi \cos \lambda) d\lambda d\phi dp + 1.10R \int \int p_s \sin \phi \cos^2 \phi \sin \lambda d\lambda d\phi \right] \\
 \frac{\Delta \text{LOD}}{\text{LOD}_0} &= \chi_3 = \frac{R^3}{C_{mg}} \left[\frac{0.997}{\Omega} \int \int \int u \cos^2 \phi d\lambda d\phi dp + R \int \int p_s \cos^3 \phi d\lambda d\phi \right]
 \end{aligned}$$

χ_1

χ_2

χ_3



Assimilating Earth Rotation Using DART-CAM

3 integral observations of the state.

χ_1, χ_2, χ_3

χ_1, χ_2, χ_3

χ_1, χ_2, χ_3



EnKF

EnKF

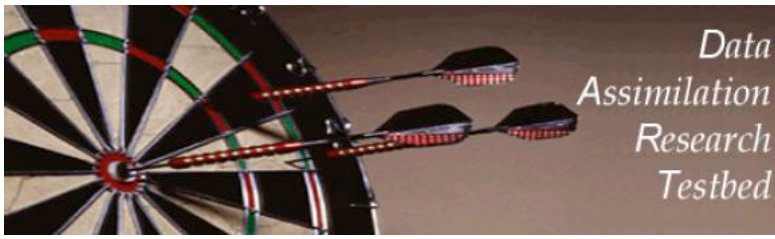
EnKF

64-Member climatological ensemble

Adjust
 u, v, p_s

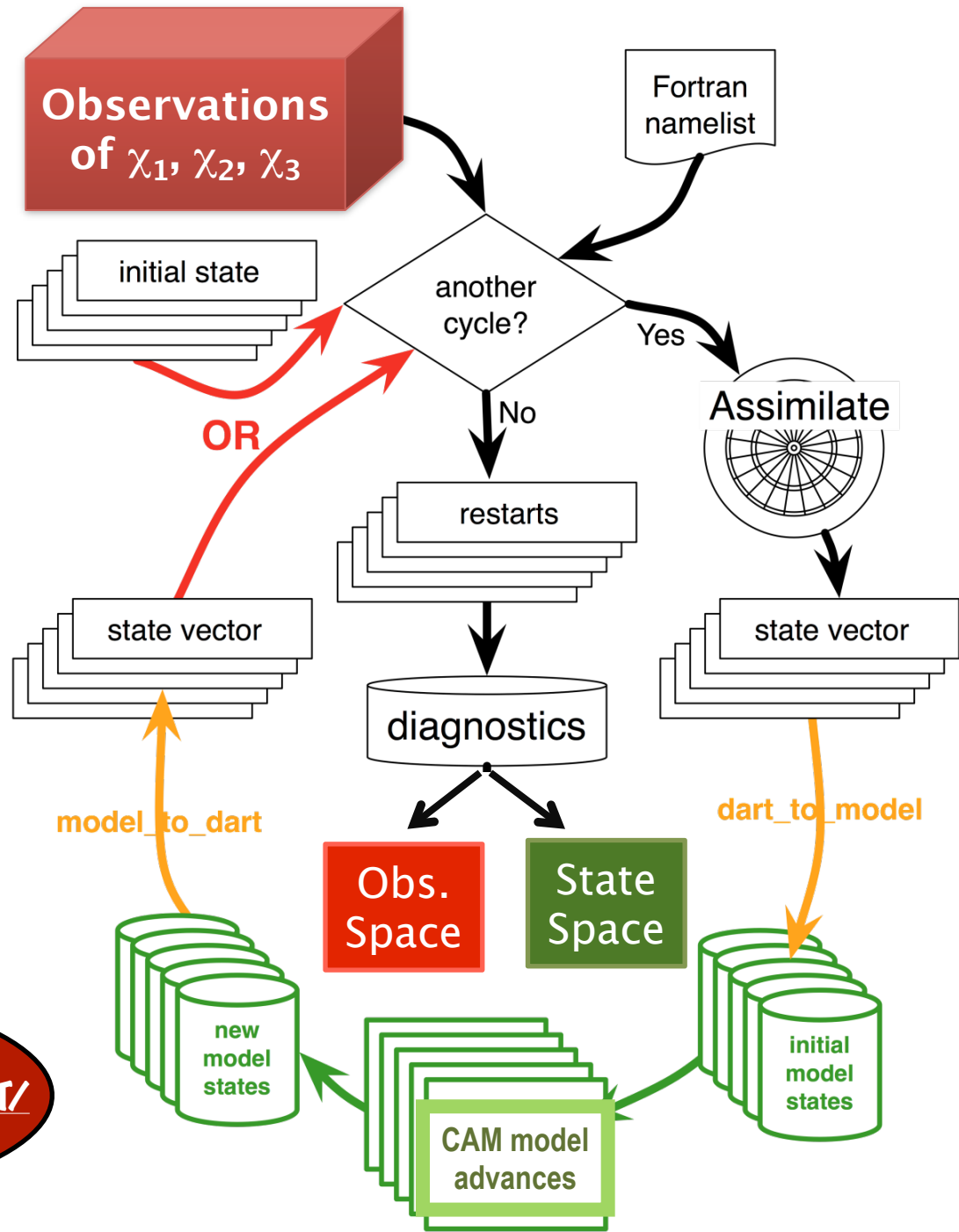
Adjust
 u, v, p_s

Adjust
 u, v, p_s

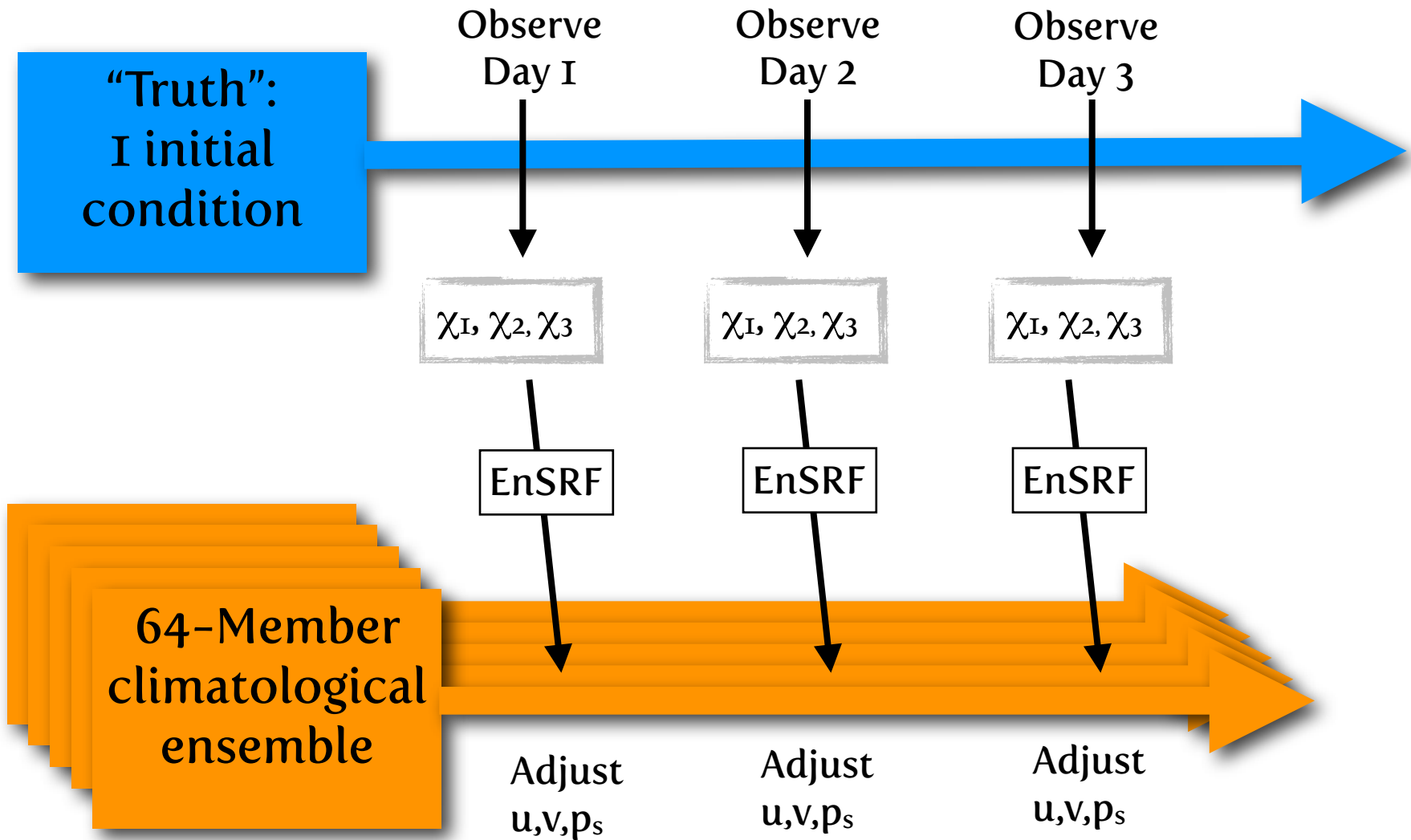


The Data Assimilation Research Testbed (DART)

Anderson et al. (2009)
<http://www.image.ucar.edu/DAReS/DART/>



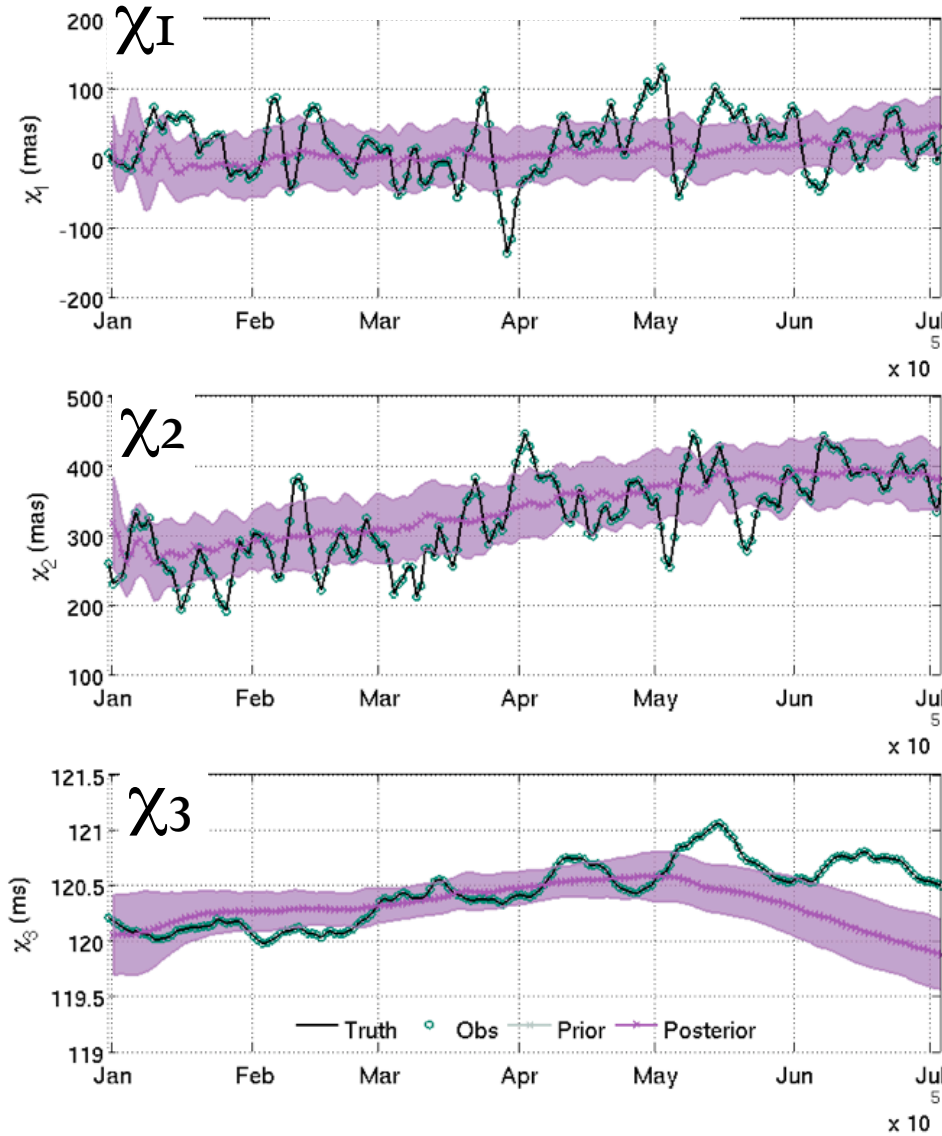
Earth Rotation OSSEs using DART



Given a perfect model and perfect observations, how well can we recover the truth?

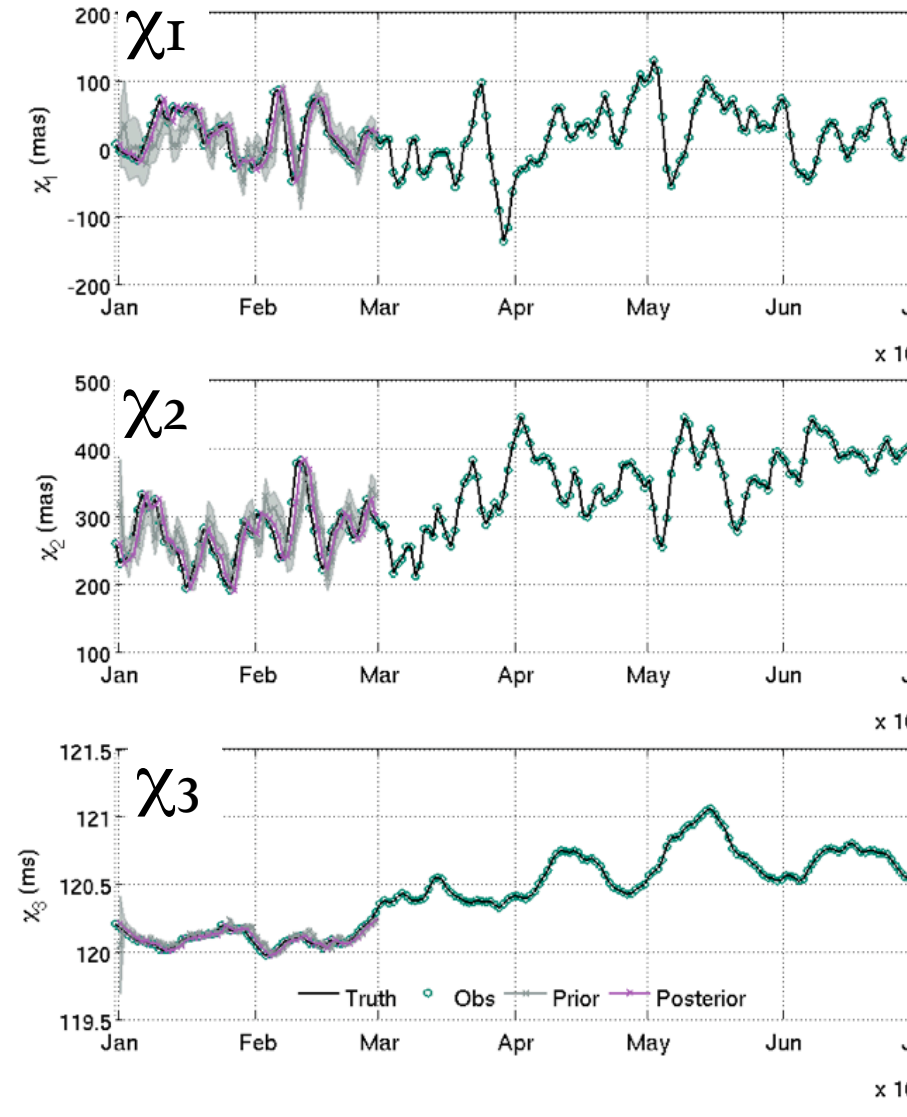
Observation Space

No Assimilation

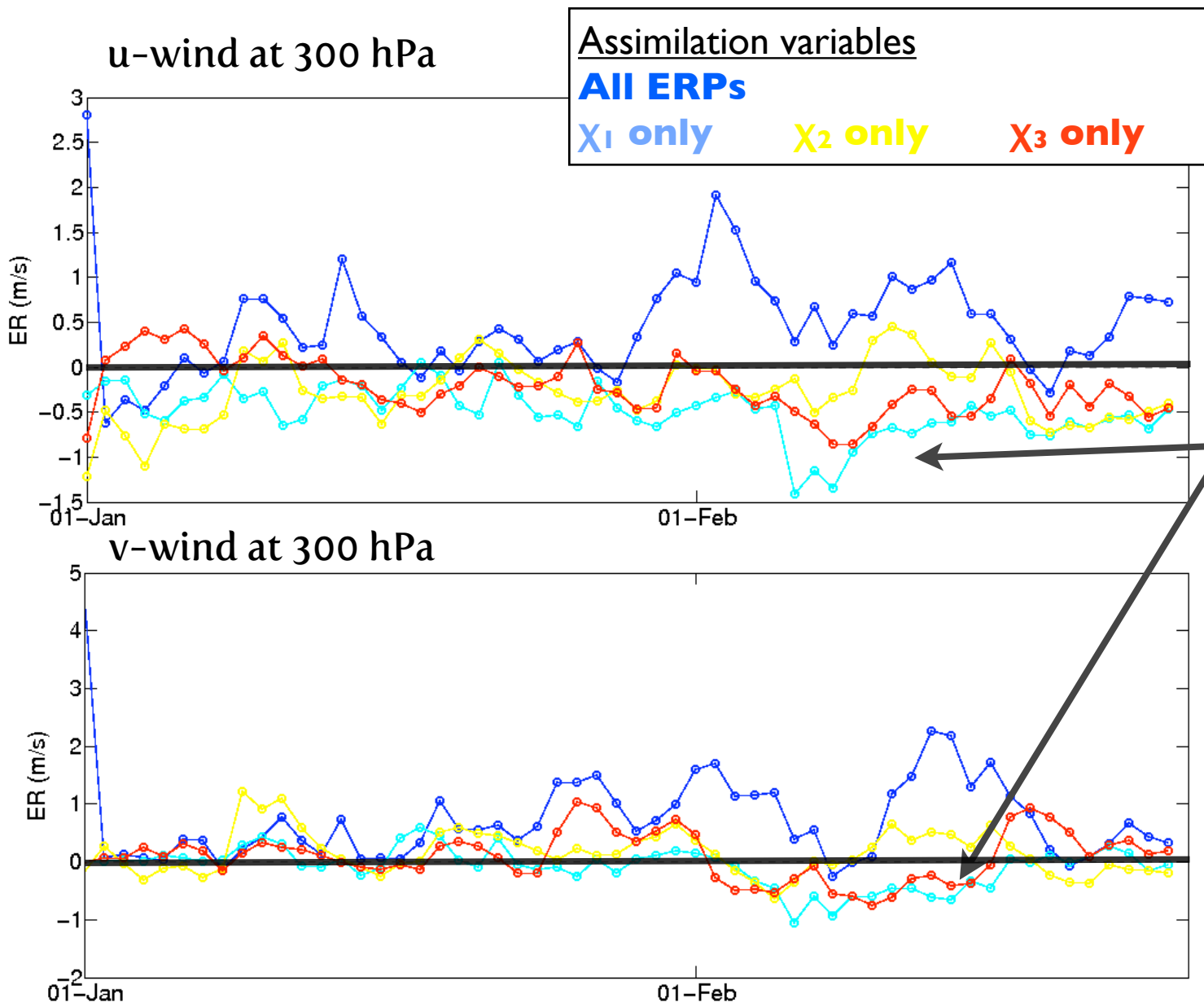


Truth Obs Prior Posterior

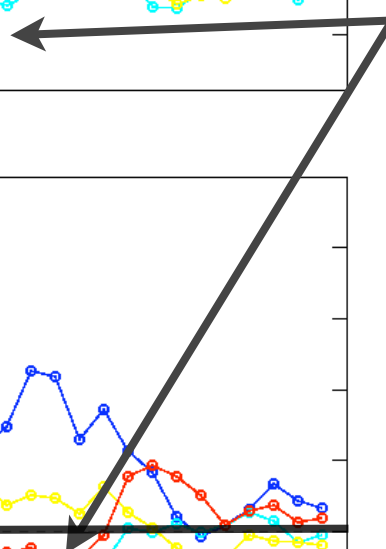
With Assimilation



State Space: Error Reduction in Time

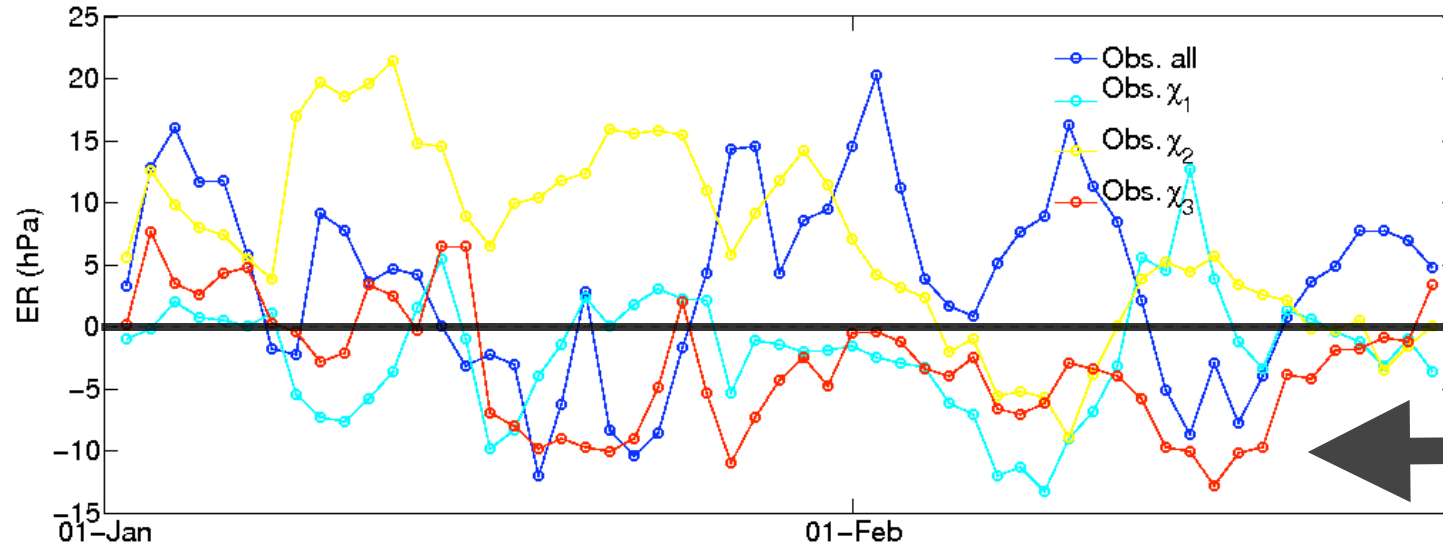


Improvement relative to no DA case: observing X_1 and X_3 yields the most improvements.



State Space: Error Reduction in Time

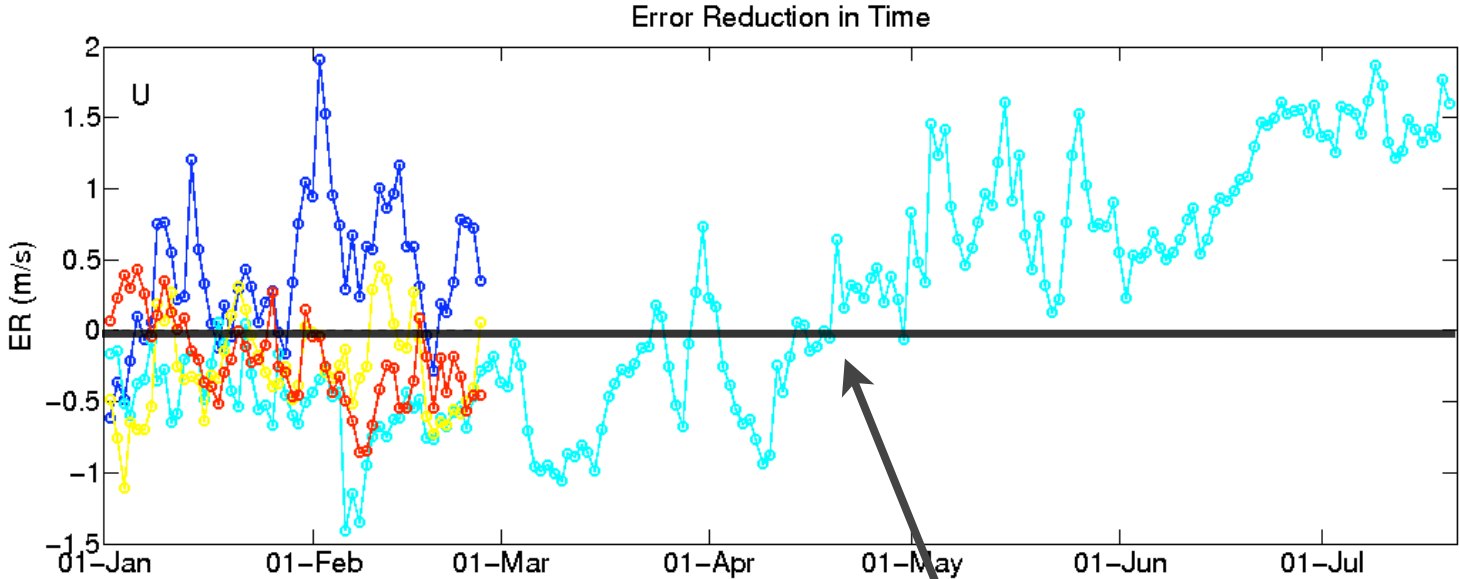
surface pressure



Some improvement relative to no-DA case.

Assimilation variables		
All ERPs		
χ_1 only	χ_2 only	χ_3 only

State Space: Error Reduction in Time

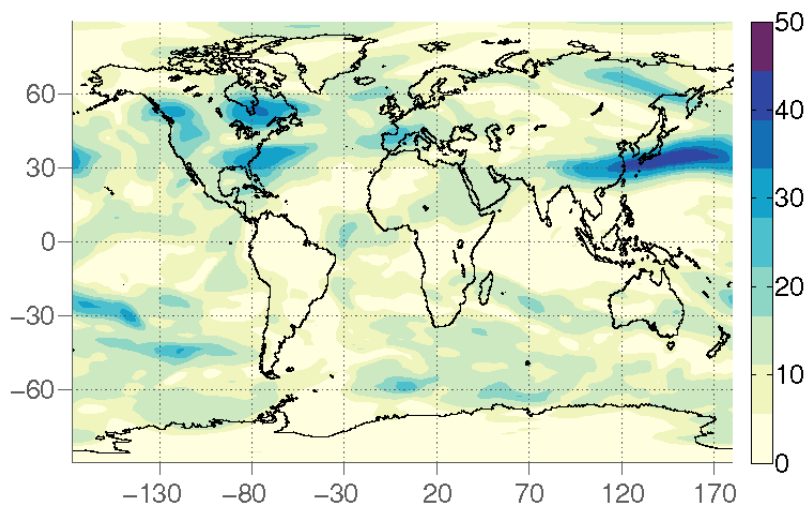


Assimilation variables
All ERPs
X₁ only **X₂ only** **X₃ only**

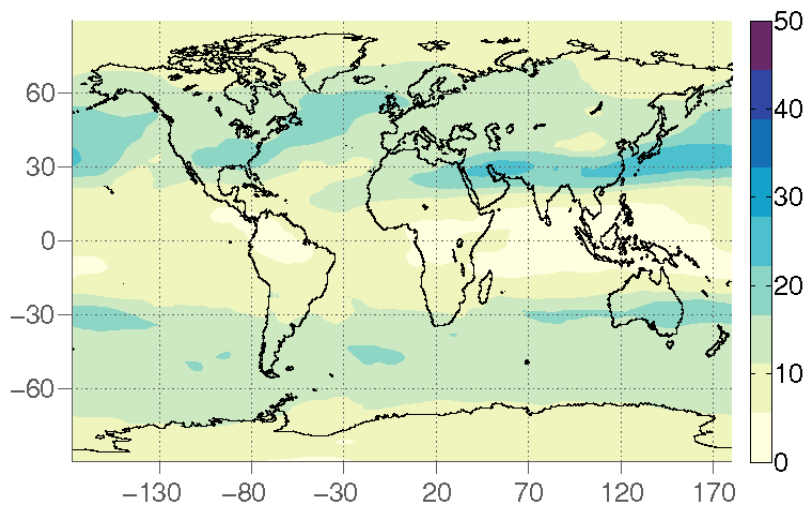
Complete filter divergence after about 4 months.

no assimilation

RMSE

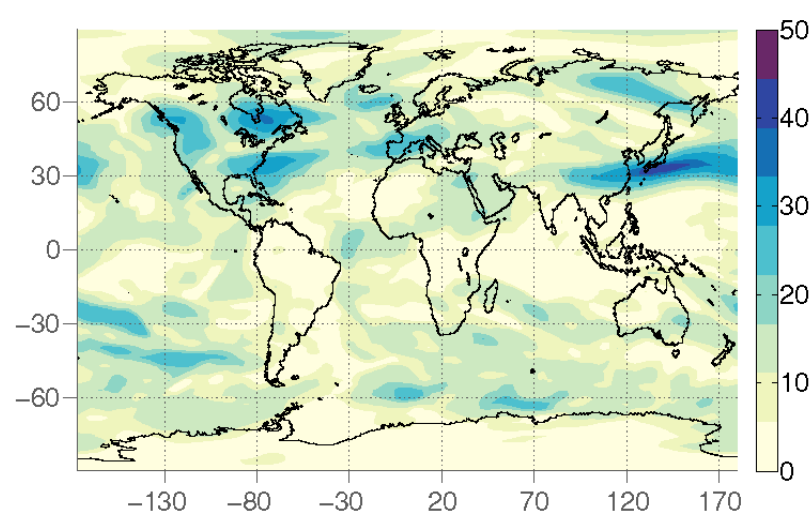


Ensemble spread

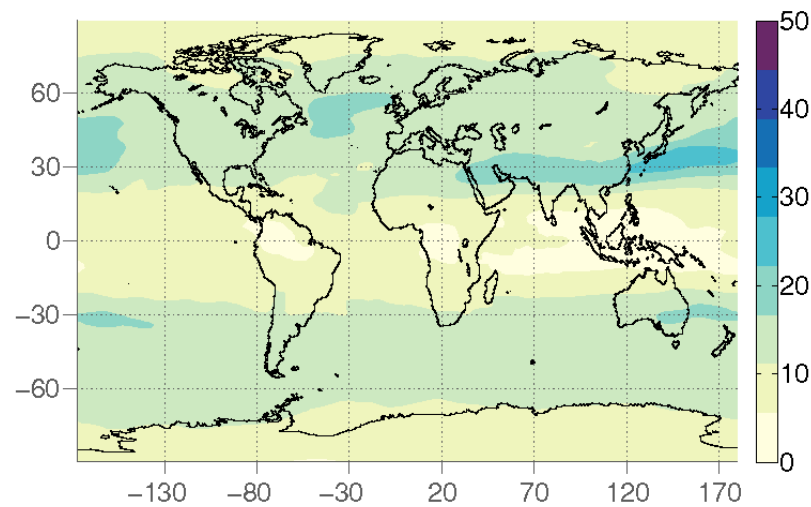


with assimilation (χ_I)

RMSE



Ensemble spread

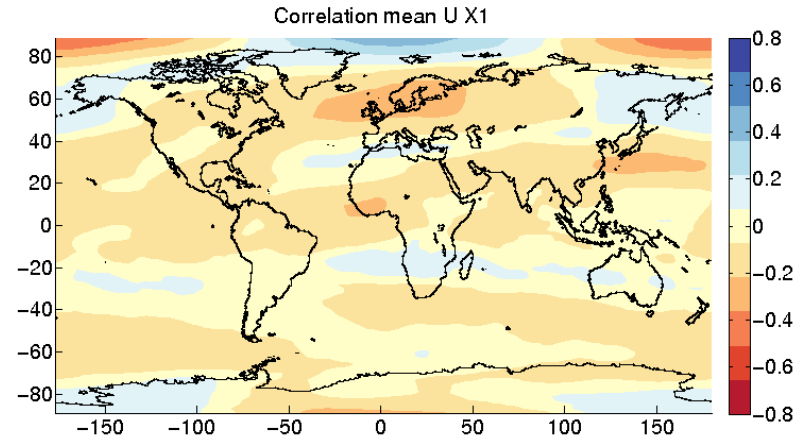


Towards localizing the Analysis Increment

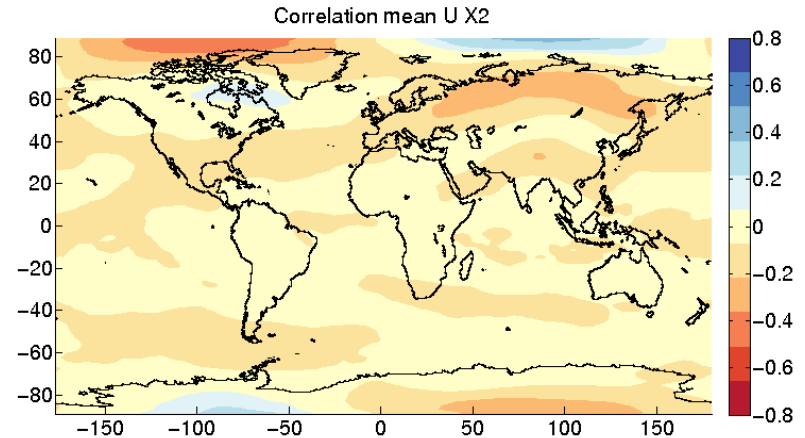
Mean **ensemble correlations**
between U-wind (300 hPa) and the
global excitation functions.

- Correlations make dynamical sense.
 - Except for strange strong signal in polar regions
 - But very small local correlations.
- >> Localization may be difficult.

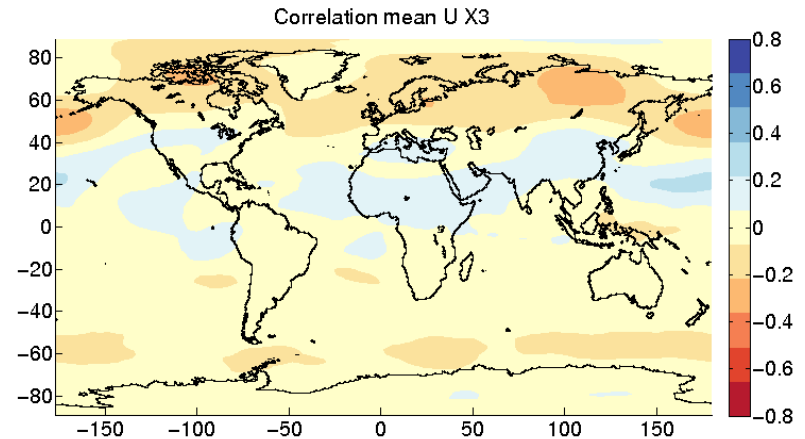
χ_I



χ_2



χ_3



Summary

- Observed **Earth Rotation Parameters** (ERPs) translate into **atmospheric excitation functions**, which are an integral constraint on the state.
- Assimilation best constrains the zonal wind field.
- Assimilating **individual** excitation functions generally improves things, but **all three together** makes the analysis worse.
- Improvement limited to ~ first 3 months of assimilation

Outlook: A New Type of Model Constraint?

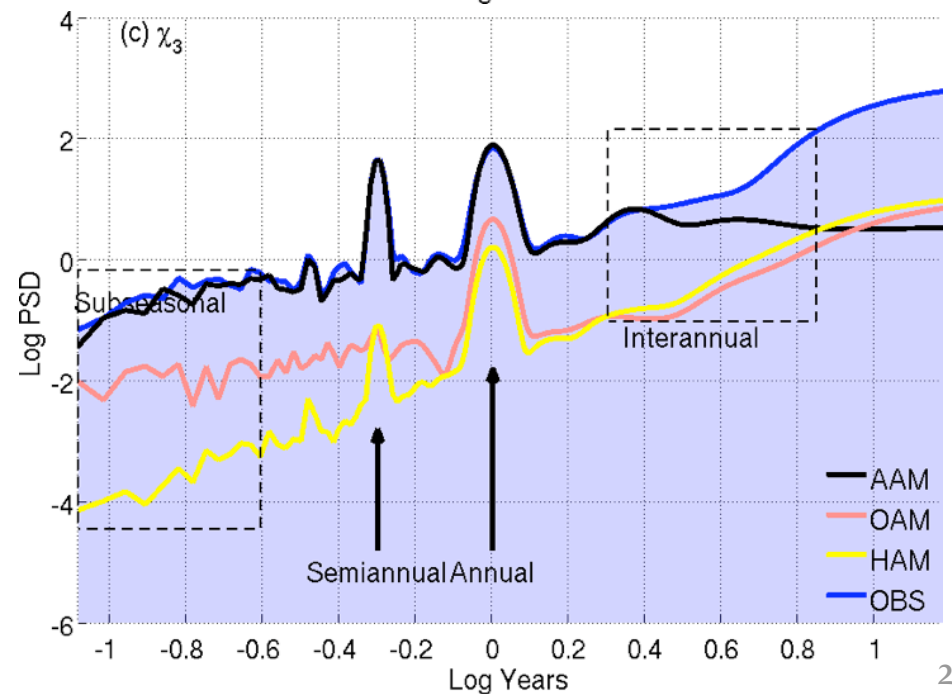
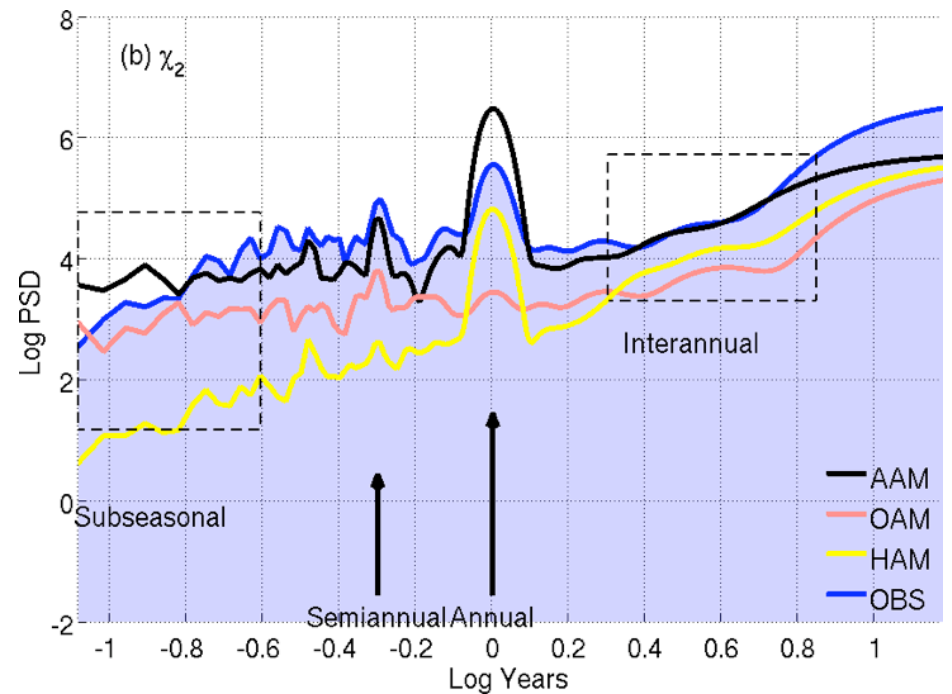
- Localization: masking out regions with spurious localization.
- A better initial ensemble: constrain with uniform local observations first, then apply ERP observations.
- Can ERPs help to capture specific events, e.g. blocking?
- Once filter divergence is taken care of: application to longer timescales (6 months - years).
- Expansion to DART-CESM and DART-WACCM (2013).

References

- **Anderson, J., et al. (2009)**, The data assimilation research testbed: A community facility, *Bull. Am. Met. Soc.*, pp. 1283–1296, doi:10.1175/2009BAMS2816.1.
- **Barnes, R., et al. (1983)**, Atmospheric angular momentum fluctuations, length-of-day changes and polar motion, *Proc. Roy. Soc. London*, 387, 31–73.
- **Gross, R. S. (2009)**, Earth rotation variations - long period, in *Geodesy, Treatise on Geophysics*, edited by T. Herring, pp. 239–294, Elsevier.
- **Dickey, J. O., et al (1991)**, Extratropical aspects of the 40-50 day oscillation in length-of-day and atmospheric angular momentum, *J. Geophys. Res.*, 96, 22,643–22,658.
- **Marcus, S. L., et al. (2012)**, Detection of the earth rotation response to a rapid fluctuation of Southern ocean circulation in november 2009, *Geophys. Res. Lett.*, 39, L04,605, doi:10.1029/2011GL050671.
- **Neef and Matthes (2012)**, Comparison of Earth rotation excitation in data-constrained and unconstrained atmosphere models, *J. Geophys. Res.*, 117, D02(107), doi: 10.1029/2011JD016555.
- **Raeder, K. et al. (2012)**, An Ensemble Data Assimilation System for CESM Atmospheric Models. *J. Clim.* doi:10.1175/JCLI-D-11-00395.1, in press.
- DART Website: <http://www.image.ucar.edu/DAReS/DART/>

Extras

Role of the Atmosphere in Excitation of AAM



Earth Angular Momentum

$$H_i(t) = I_{ij}(t)\omega_j(t) + h_j(t)$$

moment of inertia:
Depends on distribution of
mass around the Earth

relative angular
momentum:
Movements relative to the
the rotation vector ω

$$\frac{d\vec{H}(t)}{dt} = \vec{\tau} \rightarrow \boxed{d(I_{ij}\omega_j + h_i)/dt + \epsilon_{ijk}\omega_j(I_{kl}\omega_l + h_k) = \tau_i}$$

Liouville equation

If net external torques are zero, changes in relative AM and mass distribution are evened out by changes in the rotation vector.

Changes in Earth Angular Momentum

$$d(I_{ij}\omega_j + h_i)/dt + \epsilon_{ijk}\omega_j(I_{kl}\omega_l + h_k) = \tau_i$$

* Now assume very small perturbations in the MOI and relative AM
(in each vector component!)

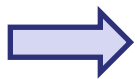
$$I_{ij}(t) = \begin{pmatrix} A & 0 & 0 \\ 0 & B & 0 \\ 0 & 0 & C \end{pmatrix} + \Delta I_{ij}(t) \quad \begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \end{pmatrix} = \begin{pmatrix} m_1 \\ m_2 \\ 1 + m_3 \end{pmatrix} \Omega$$

$$\dot{m}_1/\sigma_c + m_2 = \chi_2 - \dot{\chi}_1/\Omega$$

$$\dot{m}_2/\sigma_c - m_1 = -\chi_1 - \dot{\chi}_2/\Omega$$

$$\dot{m}_3 = -\dot{\chi}_3$$

Excitation functions χ_i :
nondimensionalized angular
momentum
exchange with Earth's fluid
shell



Atmospheric Angular Momentum

$$\begin{aligned}
 p_1 + \frac{\dot{p}_2}{\sigma_0} &= \chi_1 \\
 -p_2 + \frac{\dot{p}_2}{\sigma_0} &= \chi_2 \\
 \frac{\Delta \text{LOD}}{\text{LOD}_0} &= \Delta \chi_3
 \end{aligned}$$

Mass terms
(moment of inertia)

Motion terms
(AM relative to Earth)

$$\begin{aligned}
 \chi_1(t) &= \frac{1.608}{\Omega(C - A')} [0.684\Omega\Delta I_{13}(t) + \Delta \mathbf{h}(t)] \\
 \chi_2(t) &= \frac{1.608}{\Omega(C - A')} [0.684\Omega\Delta I_{23}(t) + \Delta \mathbf{h}(t)] \\
 \chi_3(t) &= \frac{0.997}{\Omega C_m} [0.750\Omega\Delta I_{33}(t) + \Delta h_{33}(t)]
 \end{aligned}$$

$$\begin{aligned}
 I_{13} &= - \int R^2 \cos \phi \sin \phi \cos \lambda dM \\
 I_{23} &= - \int R^2 \cos \phi \sin \phi \sin \lambda dM \\
 I_{33} &= \int R^2 \cos^2 \phi dM \\
 h_1 &= - \int R [u \sin \phi \cos \lambda - v \sin \lambda] dM \\
 h_2 &= - \int R [u \sin \phi \sin \lambda + v \cos \lambda] dM \\
 h_3 &= \int Ru \cos \phi dM
 \end{aligned}$$

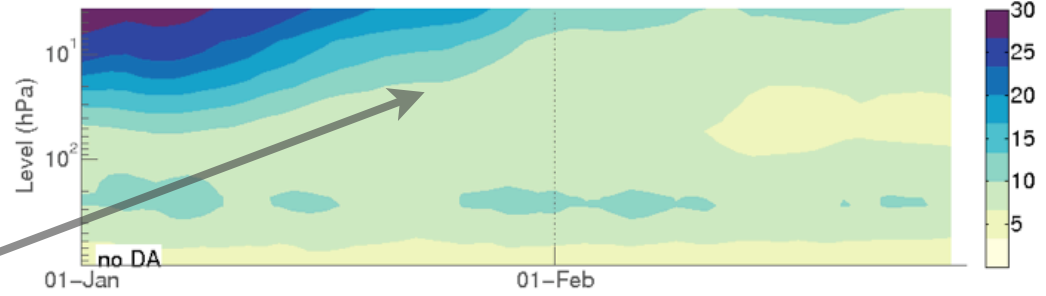
State Space Error

RMSE of u-wind at 300 hPa

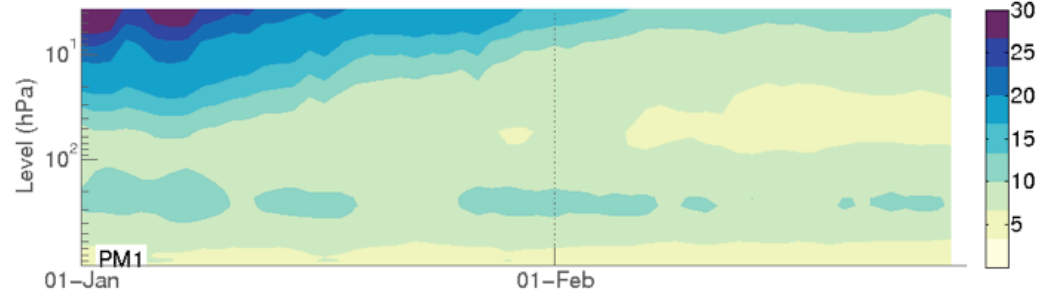
Upper level damping in CAM gets rid of initial ensemble spread.

Initial ensemble bias in the stratosphere reduced faster with obs of χ_2 and χ_3 (!?)

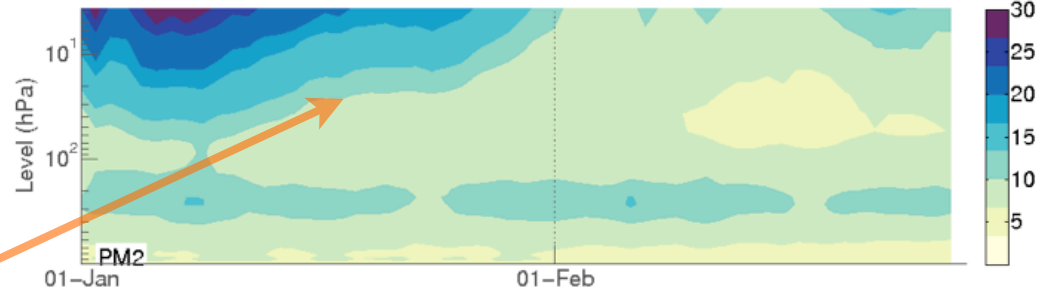
no DA



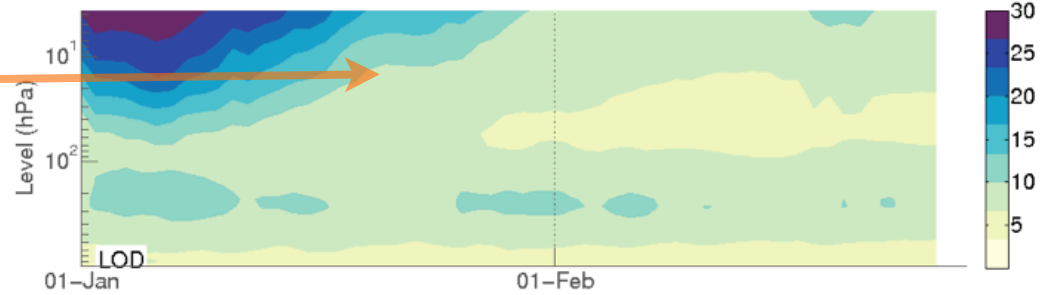
χ_I obs



χ_2 obs

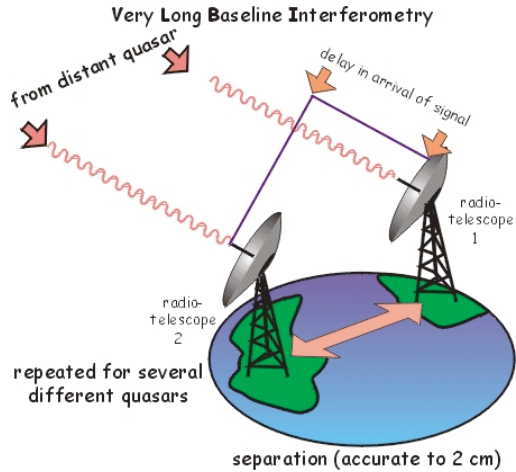


χ_3 obs



LOD

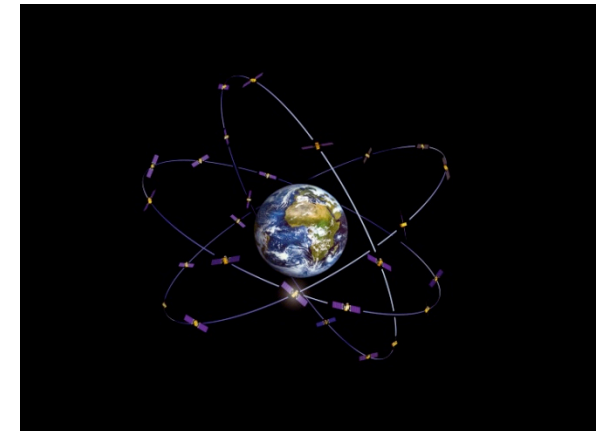
Earth Rotation Measurements



Very Long Baseline Interferometry (VLBI)



Satellite & Lunar Laser Ranging (SLR, LLR)

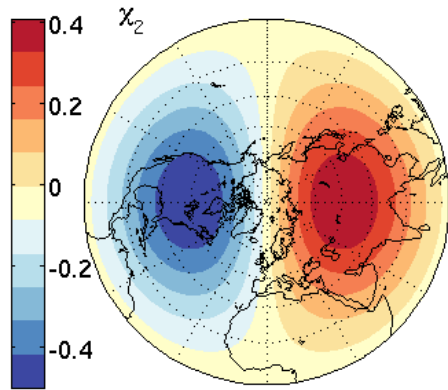


Global Positioning System (GPS)

Two angles of
Polar Motion
 p_1, p_2

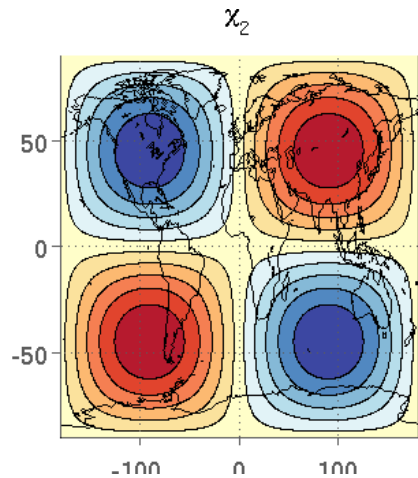
Length-of-day
anomalies
LOD

Localization of the analysis increment around the transfer function maxima

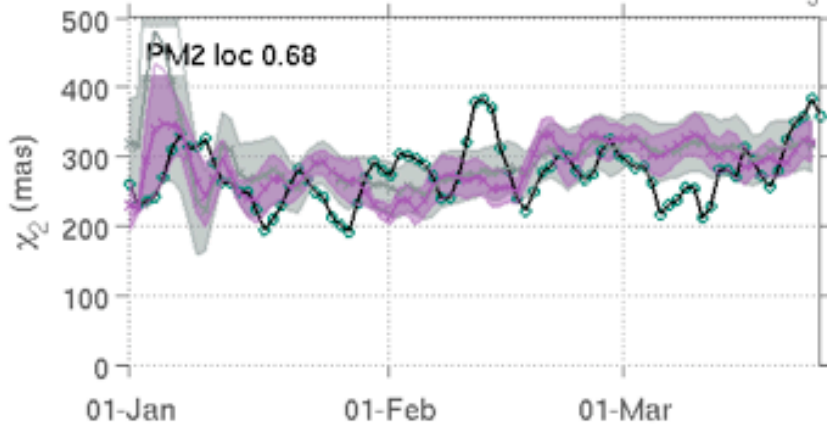
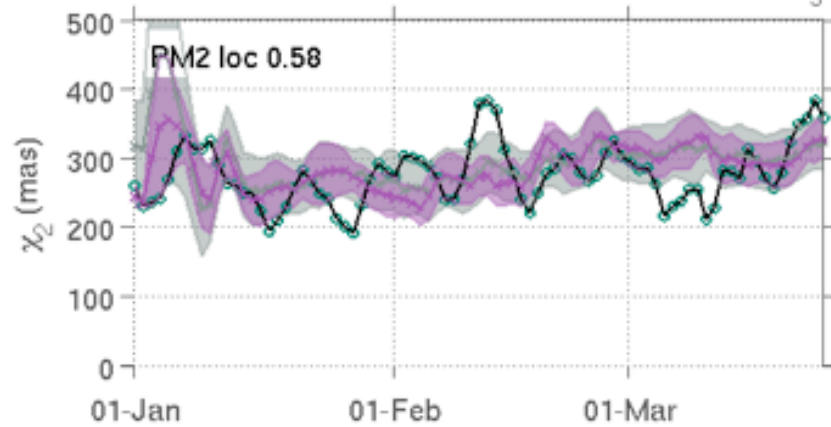
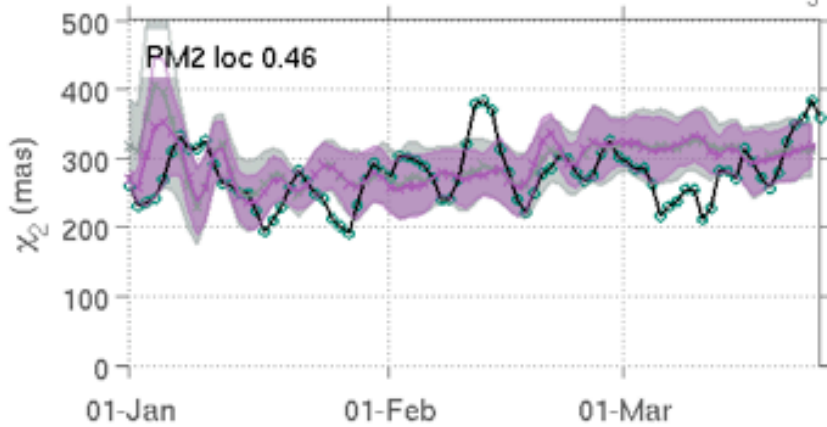
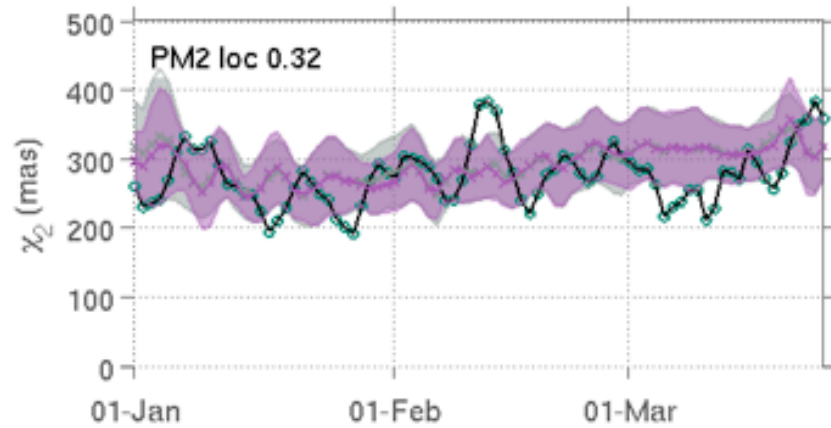
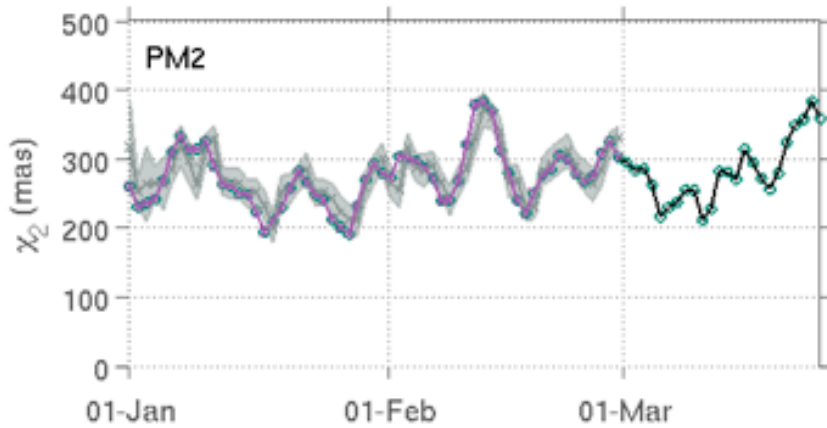


Idea:

Observing only χ_2 , localize the increment where the integral most strongly weights zonal wind.



$$\chi_2^W = \frac{-1.43R^3}{\Omega(C-A)g} \int \int \int (u \sin \phi \cos \phi \sin \lambda + v \cos \phi \cos \lambda) d\lambda d\phi dp$$



Localization of the analysis increment around the transfer function maxima: it's hard to get the fit.